

# 1 **The challenge of integrating offshore wind power in the U.S. electric grid.**

## 2 **Part II: Simulation of electricity market operations.**

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9 *Keywords:* unit commitment, power flow, economic dispatch, uncertainty, PJM.

### 10 *Highlights:*

- 11 1. Smart-ISO, a simulator of the PJM planning process, is developed, tested, and evaluated.
- 12 2. Injecting large amounts of offshore wind power (36 GW) in the current electricity grid is feasible  
13 with current planning process and current wind forecast errors simply via additional reserves;
- 14 3. With perfect wind forecasts, at least twice as much offshore wind power can be integrated with  
15 less than half of the reserves than with the current wind forecast errors.

16 *Word count:* 6975.

### 17 **Abstract**

18 The purpose of this two-part study is to analyze large penetrations of offshore wind power into the grid  
19 of a large Regional Transmission Organization (RTO), using the case of the grid operated by PJM  
20 Interconnection in the northeastern U.S. Part I of the study introduces the wind forecast error model  
21 and Part II, this paper, describes Smart-ISO, our simulator of PJM's planning process for generator  
22 scheduling, including day-ahead and intermediate-term commitments to energy generators and real-  
23 time economic dispatch. Using a carefully calibrated model of the PJM grid and realistic models of  
24 offshore wind (described in Part I), we show that, except in summer, an unconstrained transmission grid  
25 can meet the load at five build-out levels spanning 7 to 70 GW of capacity, with the addition of at most 1  
26 to 8 GW of reserves.

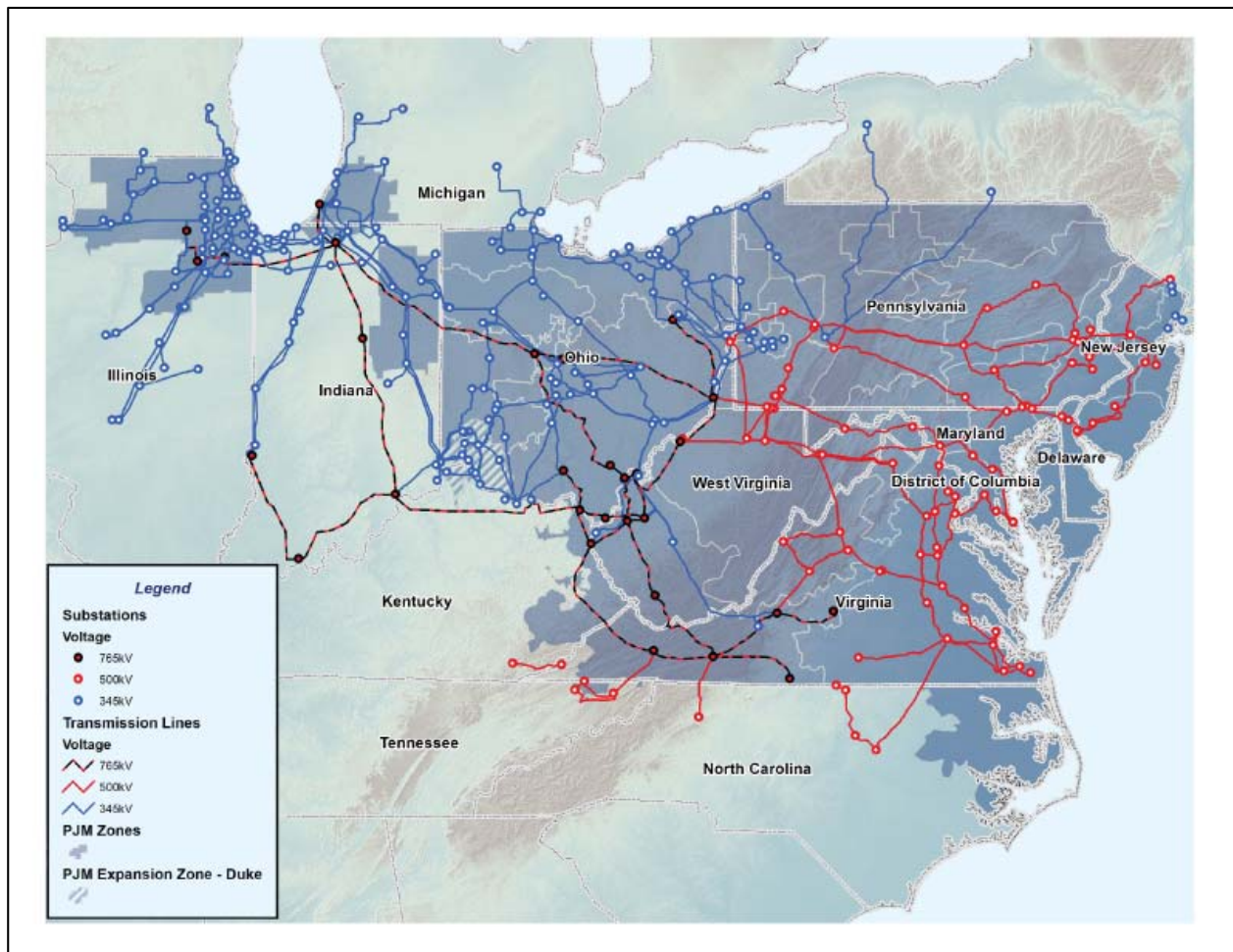
27 In the summer, the combination of high load and variable winds is challenging. We find that the  
28 simulated grid can handle up through build-out level 3 (36 GW of offshore wind capacity), with 8 GW of  
29 reserves and without any generation shortage. For comparison, when Smart-ISO is run with perfect  
30 forecasts, all five build-out levels, up to 70 GW of wind, can be integrated in all seasons with at most 3  
31 GW of reserves. This reinforces the importance of accurate wind forecasts. At build-out level 3, energy  
32 from wind would satisfy between 11 and 20% of the demand for electricity and settlement prices could

33 be reduced by up to 24%, though in the summer peak they could actually increase by up to 6%. CO<sub>2</sub>  
 34 emissions are reduced by 19-40%, SO<sub>2</sub> emissions by 21-43%, and NOx emissions by 13-37%.

35 This study finds that integrating up to 36 GW of offshore wind is feasible in PJM with today's  
 36 transmission grid, generation fleet, and today's planning policies with the addition of 8 GW of reserves.  
 37 Above that, PJM would require additional investments in fast-ramping gas turbines, storage for  
 38 smoothing fast-ramping events, and/or other strategies such as demand response.

39 **1 Introduction**

40 PJM Interconnection is a regional transmission organization (RTO) that coordinates the movement of  
 41 wholesale electricity serving 13 states and the District of Columbia, covering from the mid-Atlantic  
 42 region out to Chicago (PJM Interconnection 2014). Acting as a neutral, independent party, PJM operates  
 43 a competitive wholesale electricity market and manages the high-voltage electricity transmission grid to  
 44 ensure reliability for more than 61 million people. Figure 1 shows the geographical area covered by PJM  
 45 and the high-voltage backbone (345 kV and higher) of its transmission grid.



46

47

**Figure 1: PJM high-voltage backbone.**

48 At the end of 2013, the total installed capacity within the PJM market was about 183 Gigawatts (GW)  
 49 and the peak load during the year was over 157 GW (Monitoring Analytics 2014). The yearly generation  
 50 in PJM by percentage of each fuel source between 2010 and 2013 is shown in Table I (Monitoring  
 51 Analytics 2011, 2012, 2013, 2014).

52 **Table I: PJM actual generation by fuel source (%) between 2010 and 2013**

<b>Fuel Source</b>	<b>2010</b>	<b>2011</b>	<b>2012</b>	<b>2013</b>
<b>Coal</b>	49.3	47.1	42.1	44.3
<b>Nuclear</b>	34.6	34.5	34.6	34.8
<b>Gas</b>	11.7	14.0	18.8	16.3
<b>Hydroelectric</b>	2.0	1.9	1.6	1.8
<b>Wind</b>	1.2	1.4	1.6	1.9
<b>Other</b>	1.2	1.1	1.3	0.9

53

54 The basic functions of PJM comprise grid operations (supply/demand balance and transmission  
 55 monitoring), market operations (managing open markets for energy, capacity and ancillary services) and  
 56 regional planning (15-year look-ahead) (PJM Interconnection 2014). Our interest in this paper is to  
 57 analyze the ability of the energy market and the transmission grid within the PJM area to integrate non-  
 58 dispatchable generation in quantities much larger than the current levels. As indicated in Table I, in 2013  
 59 wind power corresponded to less than 2% of the total generation. The Mid-Atlantic offshore wind power  
 60 production proposed and modeled in Part I of this paper (Archer et al. 2015) would bring that fraction to  
 61 as much as 28% at certain times of the year, thus raising the question of how to manage the generation  
 62 schedule and the transmission grid capacity under such a scenario.

63 In order to answer this question, we introduce SMART-ISO, a simulator of the market operations of PJM,  
 64 including the transmission grid. Developed at PENS Lab at Princeton University, SMART-ISO is a  
 65 detailed model of the PJM planning process designed specifically to model the variability and  
 66 uncertainty from high penetrations of renewables. It captures the timing of information and decisions,  
 67 stepping forward in 5-minute increments to capture the effect of ramping constraints during rapid  
 68 changes in wind energy. Considerable care was invested to capture the accuracy of wind forecasts using  
 69 information from PJM's forecasts of their own wind farms, as detailed in Part I of this two-part article.

## 70 **2 The SMART-ISO model**

71 SMART-ISO is a simulator of the market operations of PJM that aims to strike a balance between  
 72 detailed representation of the system and computational performance. It comprises three optimization  
 73 models embedded within a simulation model that captures the nested decision-making process:

- 74 1. Day-ahead unit commitment (DA-UC) model.
- 75 2. Intermediate-term unit commitment (IT-UC) model.
- 76 3. Real-time economic dispatch.

77 Accurate modeling of the nesting of these three models is a central (and powerful) tool used by ISOs to  
 78 adapt to uncertainty. In SMART-ISO all three optimization models include a DC approximation of the  
 79 power flow. In addition, an AC power flow model is run after both the intermediate-term UC and the  
 80 real-time economic dispatch models in order to verify the electrical stability of the grid.

81 The simulator takes as inputs:

- 82 1. The list of generators available for scheduling in the PJM area (including all relevant operational  
 83 and economic parameters).
- 84 2. The transmission grid (buses and lines), including relevant transmission parameters.
- 85 3. Historical (and/or simulated) time series of loads (both active and reactive) at the bus level over  
 86 the simulation horizon.
- 87 4. Rolling time series forecasts of non-dispatchable generation (e.g. wind) over the same horizon.
- 88 5. Historical (and/or simulated) time series of non-dispatchable generation.

89 The forecasted time series are used in the scheduling models (day-ahead and intermediate-term UC's),  
 90 whereas the historical or simulated time series are used in the economic dispatch model.

91 The list of generators available in the simulator included 830 units, which comprised 97.8% of the  
 92 installed capacity in 2010. These generators were partitioned into four categories: (1) *must-run*, which  
 93 include all nuclear-fueled generators and those (predominantly coal-fueled) with notification plus warm-  
 94 up times above 32 hours; (2) *slow*, which include all generators with notification plus warm-up times  
 95 between 2 and 32 hours; (3) *fast*, which include those with notification plus warm-up times below 2  
 96 hours; and (4) *other*, which include hydro, pumped storage, and wind. The generators in the categories  
 97 *must-run* and *other* are assumed to be always on. Therefore only the *slow* and *fast* generators are  
 98 scheduled in the unit commitment models.

99 PJM's transmission grid comprised over 9,000 buses and 11,500 branches in 2010. Though feasible,  
 100 running the unit commitment and economic dispatch models with a full-size integrated grid has  
 101 significant computational costs. To strike a balance between grid representation and computational  
 102 complexity, we created multiple aggregate versions of the grid, including only the buses at or above a  
 103 given voltage. SMART-ISO can run the different models at different levels of aggregation, but we  
 104 recommend running the unit commitment models at higher aggregation level(s) than the economic  
 105 dispatch model. Table II displays the levels of grid aggregation available in SMART-ISO, with their  
 106 respective dimensions in terms of the total number of buses and branches. In the runs performed in this  
 107 study, we used the 315-kV grid for unit commitment (both day-ahead and intermediate-term) and the  
 108 220-kV grid for economic dispatch.

109 **Table II: Grid aggregation levels available in SMART-ISO. Column "0" includes all buses and all**  
 110 **branches.**

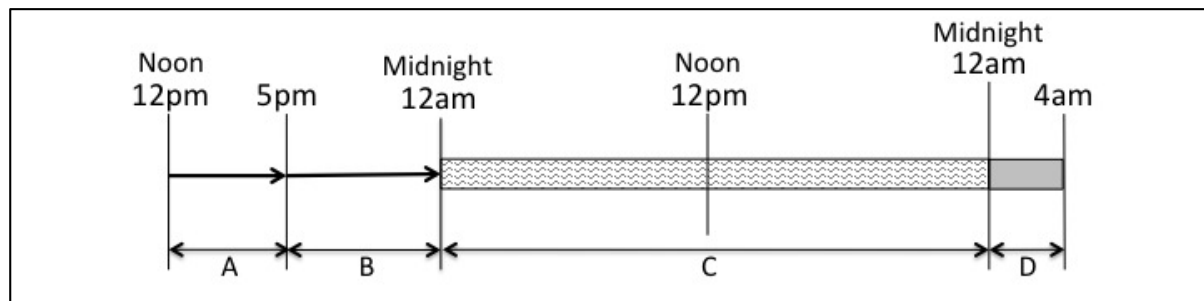
Minimum Voltage (kV)	0	69	72	118	220	315	500
# of Buses	9,154	5,881	4,829	3,950	1,360	354	131
# of Branches	11,840	7,750	6,260	5,210	1,715	454	159

111 Special care was taken within SMART-ISO to closely match PJM's *lead times* between *when a decision is*  
 112 *made* (e.g. when a unit commitment model runs) and *when it is implemented*. Not surprisingly, lead  
 113 times highlight the importance of the quality of the forecasts, especially for the intermediate-term unit  
 114 commitment model where even hour-ahead projections can be quite poor. As this article will show,  
 115 forecasting errors proved to be the major factor limiting the absorption of high penetrations of offshore  
 116 wind.

117 Typically we run SMART-ISO for a simulation horizon of 8 days, where the first day is discarded to avoid  
 118 any initialization bias. Each of the three optimization models is run sequentially over the entire  
 119 simulation horizon, with their different planning horizons and time scales nested and synchronized. The  
 120 simulation is repeated for as many sample paths of the random realizations as desired. In the next  
 121 subsections we briefly describe some details of each one of the optimization models and the power flow  
 122 models, as well as the main policy to deal with uncertainty in unit commitment.

## 123 2.1 Day-ahead unit commitment model

124 The day-ahead UC model in SMART-ISO runs once every 24 hours, at noon, similarly to how it actually  
 125 runs in PJM. Its planning horizon spans 40 hours in hourly time steps, starting from noon on a given day  
 126 until 4am on the second day following. Historical loads and long-term (day-ahead) forecasts of non-  
 127 dispatchable generation are used in this model. The planning horizon is functionally sub-divided into  
 128 four blocks of time, as depicted in Figure 2.



129

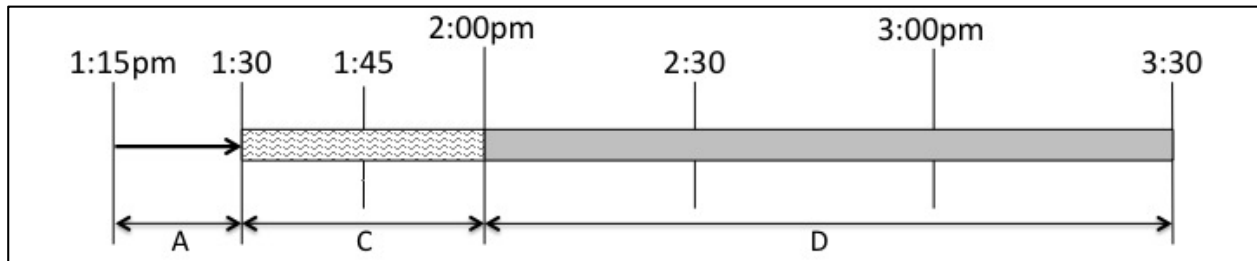
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**Figure 2: Planning horizon of day-ahead UC model.**

131 Blocks A and B correspond to the initial period of time when no generators are turned on or off because  
 132 those decisions would have been made in previous unit commitments, either the day-ahead or the  
 133 intermediate-term. During those blocks of time the UC model acts just as an economic dispatch model;  
 134 that is, it varies the amount of energy produced by each (turned-on) dispatchable generator, in order to  
 135 follow the forecasted load and adjust for the non-dispatchable generation (also forecasted). However, in  
 136 block B generators may be notified that they will have to go on or off starting from the beginning of  
 137 block C. In blocks C and D any *slow* or *fast* generator can be scheduled or unscheduled, but only the  
 138 notification and on/off decisions involving *slow* generators during periods B and C will be made effective  
 139 (that is, *locked in*), whereas decisions involving *fast* generators are finalized in the intermediate-term  
 140 model, described next. Block D is added to the time horizon to minimize end-of-horizon effects on the  
 141 decisions made at the end of block C.

142 **2.2 Intermediate-term unit commitment model**

143 The intermediate-term UC model in SMART-ISO runs twice every hour, at 15 minutes after and before  
 144 the hour. There are no on/off decisions made for *slow* generators in this model (they were all made in  
 145 the appropriate day-ahead model); only *fast* generators will be turned on or off. Short-term forecasts of  
 146 non-dispatchable generation (usually done through persistence) are used in this model. Its planning  
 147 horizon comprises 2 hours and 15 minutes, in time steps of 15 minutes, and is illustrated in Figure 3.



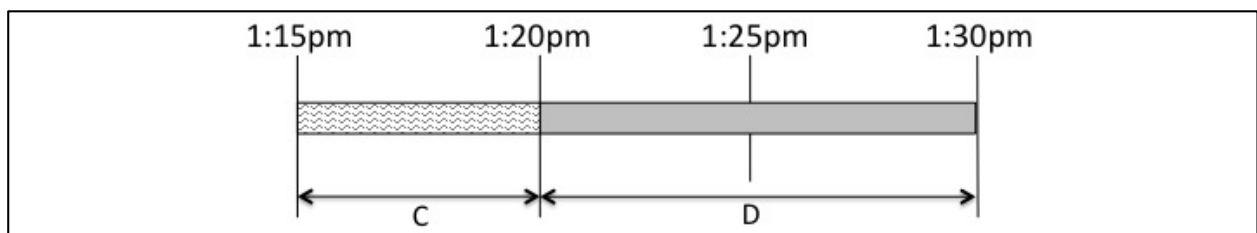
148

149 **Figure 3: Planning horizon of the intermediate-term UC model.**

150 During block A no generators can be turned on or off; they only follow the load and adjust to non-  
 151 dispatchable generation (given by short-term forecasts). *Fast* generators can be scheduled or  
 152 unscheduled in blocks C and D, though only the decisions made in block C will be locked in. Our  
 153 implementation of the intermediate-term scheduling process represents an approximation of PJM’s own  
 154 process (called *IT-SCED*), which involves running the process in 15-minute cycles, with updates every 5  
 155 minutes in case the data change. There is a variable lead-time (30 to 40 minutes) between when PJM  
 156 runs *IT-SCED* and the time of first potential dispatch of a generator (block A). After careful review with  
 157 PJM, we decided that our approximation reasonably matched their lead times, striking a balance  
 158 between model accuracy and computational complexity. The calibration results reported in a later  
 159 section further confirmed our assessment.

160 **2.3 Real-time economic dispatch model**

161 The real-time economic dispatch model in SMART-ISO runs every 5 minutes, over a planning horizon of  
 162 15 minutes, with time steps of 5 minutes, as illustrated in Figure 4. PJM also runs the economic dispatch  
 163 every 5 minutes, but over a planning horizon of 5 minutes (only one time step).



164

165 **Figure 4: Planning horizon of the real-time economic dispatch model.**

166 No generators are turned on or off in this model. Instead, generators are only modulated to follow the  
 167 actual (or simulated) load and adjust to non-dispatchable generation (also actual or simulated). The

168 generation amounts simulated in block C are kept, whereas the ones simulated in block D are discarded,  
169 as block D was added to the planning horizon of this model again to mitigate end-of-horizon biases in  
170 the calculations in block C.

## 171 **2.4 Power flow models**

172 To incorporate transmission grid constraints into SMART-ISO, we opted for implementing unit  
173 commitment and economic dispatch models that include power flow modeling as well. We used the DC  
174 approximation to solve the power flow embedded in the linear optimization problems. This is a widely  
175 used approximation for the power flow in transmission grids, since it does not require iterations (as the  
176 AC power flow does) and the optimization problem remains linear and consequently less complex (Stott  
177 et al. 2009, Hedman et al. 2011, Overbye et al. 2004). The DC approximation power flow model  
178 considers only active power and assumes that the nominal voltages remain constant.

179 However, to verify the voltage stability of the grid, and possibly correct for it, we also implemented an  
180 AC power flow model that runs once after every intermediate-term UC and once after every economic  
181 dispatch model in the simulation. If the AC power flow solution after an intermediate-term UC model  
182 shows significant voltage deviations from the nominal values (where “significant” is defined in terms of  
183 observed historical patterns), a single feedback loop will make temporary adjustments to local bus  
184 loads, and the intermediate-term UC model will be solved again, aiming to change the allocation of  
185 power generation so as to lessen the voltage deviations.

186 We found that the DC approximation can be too rigid, indicating that we might not meet power  
187 requirements (while holding voltages constant), while the AC model can flex voltages to meet loads,  
188 frequently by increasing currents. Higher currents can be tolerated for short periods of time. The greater  
189 flexibility of the AC power flow proved to be important in our studies of non-dispatchable sources,  
190 which required that we adapt to short but sudden drops in wind.

191 For this reason, the AC power flow model is solved again after each economic dispatch model run, in  
192 order to assess the overall stability and feasibility of the operation of the grid. When load is greater than  
193 generation within PJM, we refer to that as “generation shortfall.” An RTO will handle this problem with  
194 demand management, calling interruptible customers to close down, or transfers from neighboring  
195 RTOs. If there is a threat to the stability of the larger system, they would shed load by unannounced  
196 cutoffs, an emergency procedure. Without stating how PJM would respond, we simply call such cases  
197 “generation shortfall.” If the AC power flow solution does not converge or significant voltage deviations  
198 are detected, we flag the operation of the grid as “AC unstable” during that 5-minute time period. If,  
199 however, there is generation shortfall in the solution of the DC-based economic dispatch (usually an  
200 infeasible situation), but the AC power flow solution converges and is voltage-stable, then we dismiss  
201 the DC generation shortfall (that is, we declare a “no-generation shortfall” – or feasible – situation). We  
202 will allow up to 10 consecutive minutes of dismissed DC generation shortfall. If the situation persists for  
203 15 minutes or longer, then we revert the dismissal and flag the generation shortfall, regardless of the AC  
204 power flow stability.

## 205 **2.5 Reserves**

206 RTOs such as PJM use a variety of strategies to manage the uncertainties that arise in any energy  
207 system, including the hedging of decisions with the sequence of day-ahead, intermediate-term, and real-  
208 time planning, combined with the use of reserves that make it possible for PJM to respond to changing  
209 forecasts and real-time conditions that deviate from forecast. Our interest in testing much higher  
210 penetrations of wind required that we exploited these strategies, but our experiments focused primarily  
211 on increasing the availability of synchronized reserves that could be ramped (up or down) within 10  
212 minutes.

213 Our base model represented PJM’s default policy of providing enough spinning reserve to cover  
214 unexpected power imbalance equivalent to its largest generator, that is, 1300 MW. We then introduced  
215 additional reserve in the form of *fast* generators that could ramp up or down. Up-ramping was used to  
216 cover unexpected drops in wind, while down-ramping was used to take advantage of sudden surges in  
217 wind. These ramping reserves were expressed and tuned as single parameters, for each season,  
218 reflecting the differences in both the average and maximum loads, but also the types of weather  
219 encountered in each season.

220 Not surprisingly, reserves represent a powerful strategy for handling uncertainty, widely used by RTOs.  
221 An important finding of our research was that this simple industry practice could be extended to handle  
222 dramatically higher penetrations of wind than now exist, as we show below.

223 The challenge of planning market operations under uncertainty has attracted considerable attention  
224 from the algorithmic community, with special attention being given to a solution of the “stochastic unit  
225 commitment problem” (Takriti et al. 1996, Ryan et al. 2013). This is a particular algorithmic strategy  
226 developed by the stochastic programming community (Birge and Louveaux 2011), which replaces a  
227 deterministic forecast (used by all RTOs) with a set of scenarios that approximate what might happen. In  
228 this paper, we demonstrate that standard reserve policies used by RTOs are very effective at handling  
229 the uncertainty from even very high levels of renewables.

## 230 **3 Calibration of SMART-ISO**

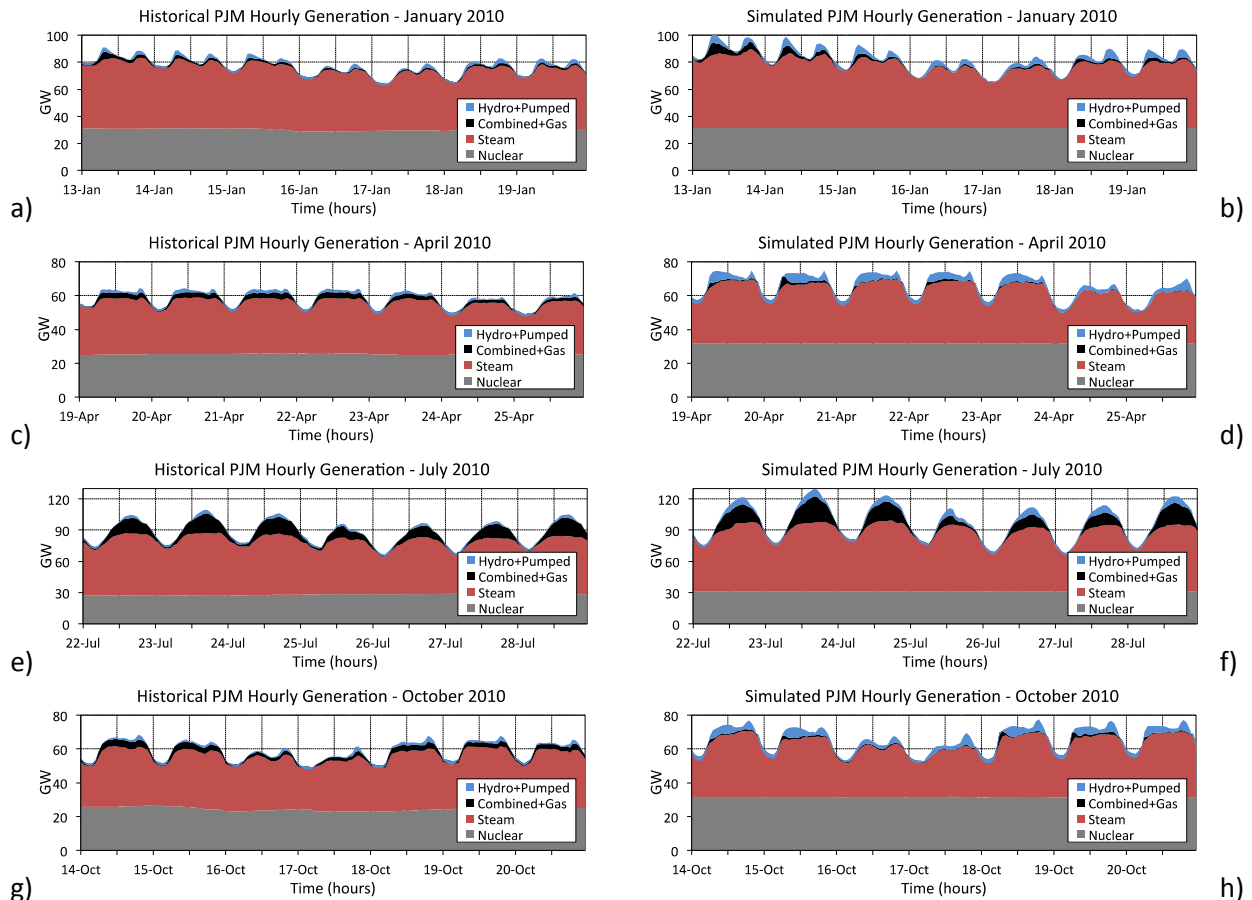
231 The first task was to calibrate SMART-ISO against a base case with no offshore wind power. We chose  
232 2010 as the base year because it was the latest year for which a complete data set of the PJM network  
233 and actual operations was available when we started the project. We chose to simulate four weeks  
234 during the year, one in each season. April and October were chosen as representative of the shoulder  
235 (lowest demand) months in spring and fall. January was chosen as representative of the winter demand,  
236 and July was picked as representative of the peak summer demand.

237 To focus on uncertainty in wind forecasts, we eliminated other sources of uncertainty from the  
238 simulation by (1) using actual (historical) time series of demand (loads) rather than long-term or short-  
239 term forecasts, (2) ignoring onshore wind and solar production, (3) ignoring potential generator and  
240 transmission failures, and (4) ignoring variations due to neighboring RTOs. Therefore, the only  
241 uncertainty present in this study comes from the forecasted offshore wind power. Similarly, we modeled



242 the same level of synchronized reserve used by PJM, which was 1300 MW (the size of their largest  
 243 generator). While this reserve would cover the loss of any one generator, we used it to respond to  
 244 uncertainty in wind forecasts as well. We also found that modest reserves were needed to deal with  
 245 what might be called “model noise” – variations in the solution arising from model truncation and from  
 246 solving large integer programs. In this section we present results on the calibration of SMART-ISO,  
 247 whereas in the next we discuss the results from the integration study.

248 We validated SMART-ISO by comparing two sets of statistics from the model to history: the hourly  
 249 generation type mix and the hourly locational marginal price (LMP) averaged over the entire grid. These  
 250 statistics were created for each of the four seasonal weeks. Figure 5 displays the plots of the historical  
 251 hourly generation type mix for each one of the four weeks (left column), placed side-by-side with the  
 252 corresponding simulated mixes (right column). We grouped the generation types in four major  
 253 categories: nuclear, steam, combined-cycle/gas-turbines, and hydroelectric/pumped-storage.

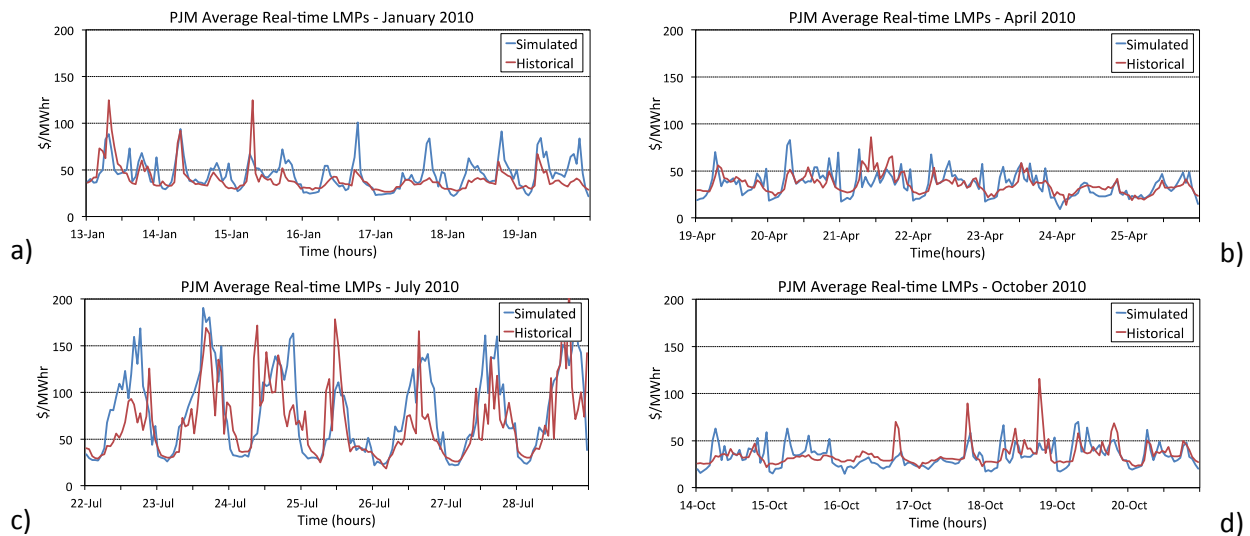


254 **Figure 5 Comparison of historical versus simulated PJM hourly generation mixes in 2010. The scale of**  
 255 **the values shown in the vertical axis (generated power) varies from month to month.**

256 We note that while we had access to detailed actual generation and load data at the bus level, we were  
 257 not able to map all buses to actual generators. As a result, our accounting of the total historical  
 258 generation is below the total load by about 10% (this explains the higher level of generation displayed in  
 259 the simulation plots). However, we can still compare the patterns of the hourly generation mix within

260 each month, which show a good match between historical and simulated results. It is noteworthy also  
 261 that the proportion of simulated generation from combined-cycle and gas turbines in the low-demand  
 262 months (April and October) is lower than the actual historical values, possibly due to the fact that  
 263 SMART-ISO does not take into consideration long-term contracts that may exist between some *fast*  
 264 generation suppliers and PJM, but schedules all *fast* generation on an hourly basis and as needed (note  
 265 this issue is *not* present in the higher-demand months of January and July). While this introduced a  
 266 modest error, it was important for us to avoid capturing long-term contracts, because we cannot  
 267 assume the same contracts would be in place as we model high penetrations of wind energy.

268 More significant, however, are the results shown in Figure 6, where we compare the locational marginal  
 269 prices (LMPs – in \$/MWhr) produced by the simulator with those observed in the actual operation of  
 270 PJM. Please note that the LMPs produced by SMART-ISO include the energy and the transmission grid  
 271 congestion costs, but not the costs due to transmission line losses or to occasional contingencies (a  
 272 failure of a generator or of a transmission line, or off-grid outages). This would explain why historical  
 273 prices might be spikier than simulated ones. In general, however, there is a remarkable agreement in  
 274 the patterns between the network-averaged LMPs produced by the simulation and those observed in  
 275 history for the four time periods in question (Figure 6).



276 **Figure 6 Comparison of historical versus simulated PJM average real-time LMPs.**

277 On the basis of these results, we conclude that SMART-ISO closely matches the behavior of PJM, since  
 278 accurate modeling of LMPs requires that all the components of the system capture real-world behavior.  
 279 We note that we achieved these results without using any tunable parameters.

#### 280 **4 Mid-Atlantic Offshore Wind Integration (MAOWIT) Study**

281 There are four core questions concerning the integration of large amounts of non-dispatchable energy  
 282 (in this case, offshore wind) into a generation and transmission market:

- 283 1. Will the existing generation capacity be able to handle the discrepancy between the forecasts  
 284 used in the commitment phase and the actual energy observed in real-time?

- 285 2. Will the *planning process* be able to handle the much higher level of variability and uncertainty  
286 (even if there is enough generation capacity)?
- 287 3. What reserve levels will be required to handle the uncertainty introduced with high  
288 penetrations of wind?
- 289 4. Will the transmission grid be able to handle the additional load?

290 In this study, offshore wind power, in five increasing levels of build-out, is assumed to be injected into  
291 the eastern side of the PJM grid through six points of interconnection on the coast, stretching from  
292 Central New Jersey to Virginia. Therefore, it is almost certain that the transmission grid along the Mid-  
293 Atlantic coast will hit capacity when significant amounts of energy from offshore wind are injected.

294 To separate the issue of grid capacity from the planning and supply of energy from a fleet of generators,  
295 we divided our study into two parts: 1) analysis with a hypothetical grid, referred to as the  
296 unconstrained grid, that has the same physical lines as the current PJM system, but thermal capacities,  
297 thus electric power carrying capacities, high enough to handle any penetration level (this is not the same  
298 as ignoring the grid, which we did not do); and 2) analysis with a grid constrained by current thermal  
299 capacities. We report on the results of these two parts in the remainder of this section.

#### 300 **4.1 Unconstrained grid, no ramp-up or -down reserves added**

301 We ran the SMART-ISO simulator over one-week horizons in each of the four seasonal months, first  
302 without any offshore wind (the “current” situation, also called build-out level 0) and then with each one  
303 of the five build-out levels of offshore wind. For each level of build-out and each month, we picked three  
304 different weeks, each exhibiting different meteorological conditions. For example, different weeks  
305 might exhibit various storm systems that introduce a variety of ramping events produced by the WRF  
306 meteorological simulator. We then used our model of forecast errors to generate seven sample paths of  
307 offshore wind for each week, thus totaling 21 sample paths for each month, or 84 sample paths overall  
308 (Archer et al. 2015). The results presented henceforth were compiled from simulations using these  
309 sample paths.

310 Table III shows the results of adding increasingly higher levels of offshore wind into the unconstrained  
311 PJM grid. The percentage of offshore wind participation in the total generation at build-out level 1  
312 ranged from 2.2% in the peak load month of July to 4.3% in the winter month of January, whereas at  
313 build-out level 5 (the highest) it ranged from 16.7% to 30%. The percentage of wind used, with respect  
314 to what was actually available, was as high as 94.8% at build-out level 1 in January, and as low as 56.4%  
315 at build-out level 5 in October.

316 The most noteworthy results in Table III, though, are the estimates of the likelihood of generation  
317 shortfall at some time during the simulated week, due to unexpected differences between the  
318 forecasted and actual wind power generation. At build-out level 1, in January and July, for instance,  
319 when the loads are higher, the probabilities that the system may operate *without* any generation  
320 shortfall during the week are much smaller than in the shoulder months of April and October. From  
321 build-out level 2 and up, in any season, it is practically certain that the PJM system as currently operated  
322 (including current reserves) will face generation shortfall at least once a week.

323 There are different ways in which the PJM market operation can be modified to try to cope with the  
 324 uncertainty in the wind power forecasts. We tested one of them (the one that is actually already used by  
 325 the ISOs to deal with uncertainties in the power generation): the addition of ramp-up and ramp-down  
 326 reserves from dispatchable (*fast*) generation. The levels of these additional reserves had to be estimated  
 327 for each build-out level and season of the year. In addition to these runs, we also performed  
 328 experiments assuming the idealized situation of having access to *perfect forecasts*, that is, day-ahead  
 329 and intermediate-term wind forecasts that are equal to the actual observed values. These experiments  
 330 allowed us to get a sense of the value of better forecasting. We refer to the latter experiments as the  
 331 *perfect forecast cases*, whereas the runs with the original forecasts are referred to as the *imperfect*  
 332 *forecast cases*.

333 **Table III: Performance metrics of the simulated, unconstrained PJM grid, with imperfect forecasts and**  
 334 **no additional reserves, after adding increasingly higher levels of offshore wind power.**

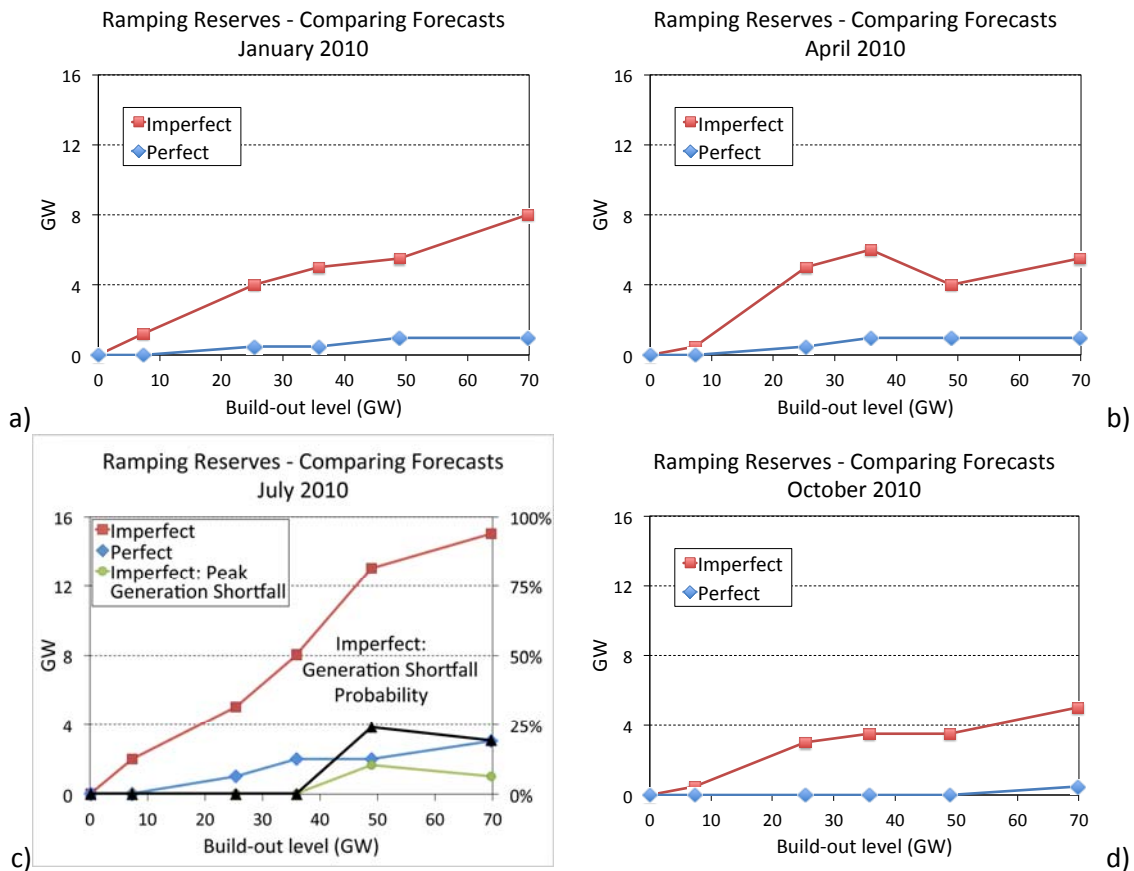
Build-out Level	Installed Capacity (GW)	Month-Year	Generation from Offshore Wind (%)	Used Wind (%)	Likelihood There Will Be Generation Shortfall at Some Time During the Week (%)	Average Peak Generation Shortfall (GW), When There Is Any Shortfall
1	7.3	Jan-10	4.3	94.8	38.1	0.6
		Apr-10	4.0	78.3	9.5	0.3
		Jul-10	2.2	92.1	81.0	2.3
		Oct-10	4.0	78.2	9.5	0.6
2	25.3	Jan-10	14.5	93.4	100.0	3.1
		Apr-10	15.1	87.7	100.0	3.8
		Jul-10	7.1	86.9	100.0	6.4
		Oct-10	15.8	90.0	100.0	2.3
3	35.8	Jan-10	20.8	93.4	100.0	5.2
		Apr-10	20.4	83.9	100.0	4.3
		Jul-10	10.3	85.6	100.0	7.7
		Oct-10	20.8	83.9	100.0	3.2
4	48.9	Jan-10	25.6	84.2	100.0	5.4
		Apr-10	24.2	74.0	100.0	4.4
		Jul-10	14.1	80.5	100.0	9.8
		Oct-10	24.1	72.1	100.0	3.9
5	69.7	Jan-10	30.0	68.7	100.0	7.4
		Apr-10	29.9	62.9	100.0	5.4
		Jul-10	16.7	68.1	100.0	12.5
		Oct-10	27.5	56.4	100.0	3.1

335

## 336 4.2 Unconstrained grid, with ramp-up and -down reserves added

337 Figure 7 shows the levels of 10-minute ramp-up and down reserves (synchronized) that were added to  
 338 the system in order to guarantee that it would operate without generation shortfall. These levels were  
 339 estimated (or “tuned”) through a series of simulation runs where we varied the amount of required  
 340 reserves until we found the approximate minimum amount, for each month and each build-out level,  
 341 such that no generation shortfall was observed in any of the 21 simulation sample paths. These reserves  
 342 are in addition to the usual PJM synchronized reserve (or spinning reserve), which is currently set at 1.3  
 343 GW (the size of the largest generator operating in the system). Each plot in Figure 7 depicts the  
 344 additional reserve level (in GW) required in that month, for each one of the five offshore wind build-out

345 levels, indicated by their respective installed capacities (in GW). Note that build-out level “0”  
 346 corresponds to the case with no offshore wind power, and thus the zero level of additional reserves  
 347 required.



348 **Figure 7 Ramping reserves needed for a range of build-outs, comparing the cases of imperfect and**  
 349 **perfect wind forecasts. For the July case (c), the right axis is the reference for generation shortfall**  
 350 **probability.**

351 Table IV shows all performance metrics of the simulated, unconstrained grid, with additional ramp-up  
 352 and down reserves, for the imperfect forecast case. With the exception of the peak summer load period,  
 353 it is possible to mitigate the uncertainty in the imperfect wind forecasts, for all build-out levels, with the  
 354 addition of synchronized reserves provided by *fast* generators. As expected, the higher the build-out  
 355 level, the larger the required reserves. For July, they amounted to over 15 GW (>20% of wind generation  
 356 *capacity*).

357 For the summer peak month, we were not able to find a level of ramp-up and down reserves that could  
 358 completely eliminate generation shortfall for build-out levels 4 and 5, *given the available fleet of gas*  
 359 *turbines*. Our conjecture is that the combination of a load increase in the mid-day peak hours with an  
 360 unexpected, steep wind power decrease at the same time creates a situation where the existing *fast*  
 361 generators might simply not have enough capacity or be fast enough to avoid generation shortfall. This  
 362 is illustrated in Figure 8, where the simulated wind power unexpectedly drops by about 25 GW within 40  
 363 minutes (bottom plot), at a time when the load is still increasing (between 1 and 2pm). This creates a

364 generation shortfall for about 35 minutes, with a peak power shortage of about 2.5 GW (top plot), *after*  
 365 the additional reserves of 13 GW have already been exhausted.

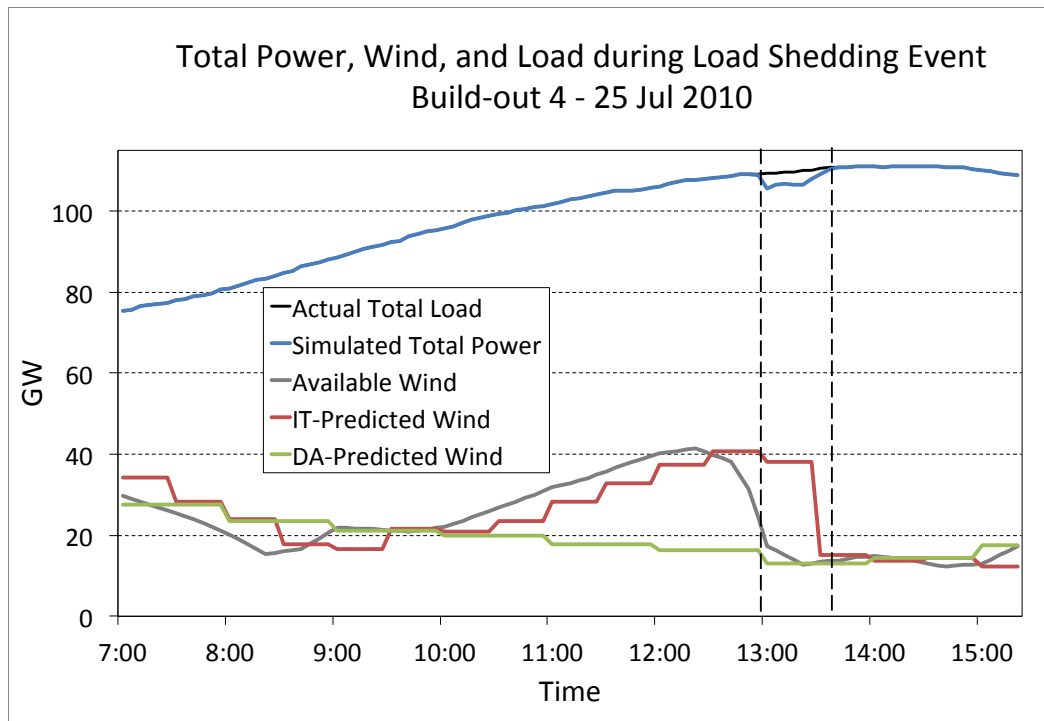
366 **Table IV: Performance metrics of the simulated, unconstrained PJM grid with imperfect forecasts after**  
 367 **adding increasingly higher levels of offshore wind power and specific ramp-up and ramp-down**  
 368 **reserves.**

Build-out Level	Installed Capacity (GW)	Month-Year	Ramping Reserves (GW)	Generation from Offshore Wind (%)	Used Wind (%)	Likelihood There Will Be Generation Shortfall at Some Time During the Week (%)	Average Peak Generation Shortfall (GW), When There Is Any Shortfall
1	7.3	Jan-10	1.2	4.3	95.0	0.0	0
		Apr-10	0.5	3.9	77.2	0.0	0
		Jul-10	2	2.3	92.5	0.0	0
		Oct-10	0.5	4.0	77.2	0.0	0
2	25.3	Jan-10	4	14.0	90.1	0.0	0
		Apr-10	5	13.5	78.6	0.0	0
		Jul-10	5	7.4	86.0	0.0	0
		Oct-10	3	15.1	85.6	0.0	0
3	35.8	Jan-10	5	20.0	90.3	0.0	0
		Apr-10	6	16.1	67.3	0.0	0
		Jul-10	8	10.8	86.2	0.0	0
		Oct-10	3.5	18.4	73.9	0.0	0
4	48.9	Jan-10	5.5	24.6	81.4	0.0	0
		Apr-10	4	21.0	62.5	0.0	0
		Jul-10	13	14.7	82.1	23.8	1.6
		Oct-10	3.5	20.5	61.2	0.0	0
5	69.7	Jan-10	8	27.8	63.8	0.0	0
		Apr-10	5.5	23.4	49.0	0.0	0
		Jul-10	15	17.4	69.6	19.1	1.0
		Oct-10	5	21.2	43.3	0.0	0

369

370 Figure 7c shows on the right-hand vertical axis the increasing probability that there will be a generation  
 371 shortfall in one week of operation in the peak summer month. The same plot also shows the average  
 372 peak generation shortfall, when there is any shortfall. For build-out level 3 in July we observed no  
 373 generation shortfall. Therefore we can say that the maximum build-out level of offshore wind that the  
 374 current PJM market can take – without any generation shortfall – and with additional synchronized  
 375 ramping reserves of up to 8 GW, is 3, which corresponds to an installed capacity of 35.8 GW.

376 On the other hand, if we had access to perfect wind forecasts in the unit commitment planning, we  
 377 would be able to handle all build-out levels of wind, including in the summer, with just nominal amounts  
 378 of additional synchronized reserves, as shown in the plots of Figure 7. In the real world there will  
 379 obviously never exist perfect wind forecasts. However, these results suggest that a *future* combination  
 380 of forecast improvements *with* additional synchronized reserves (and corresponding investments in the  
 381 grid) could potentially allow the PJM system to operate without generation shortfall, for levels of  
 382 installed offshore capacity of up to about 70 GW (which would provide for about 30% of the demand for  
 383 electricity in the winter, for example). These results highlight the importance of considering uncertainty  
 384 when managing energy from wind.



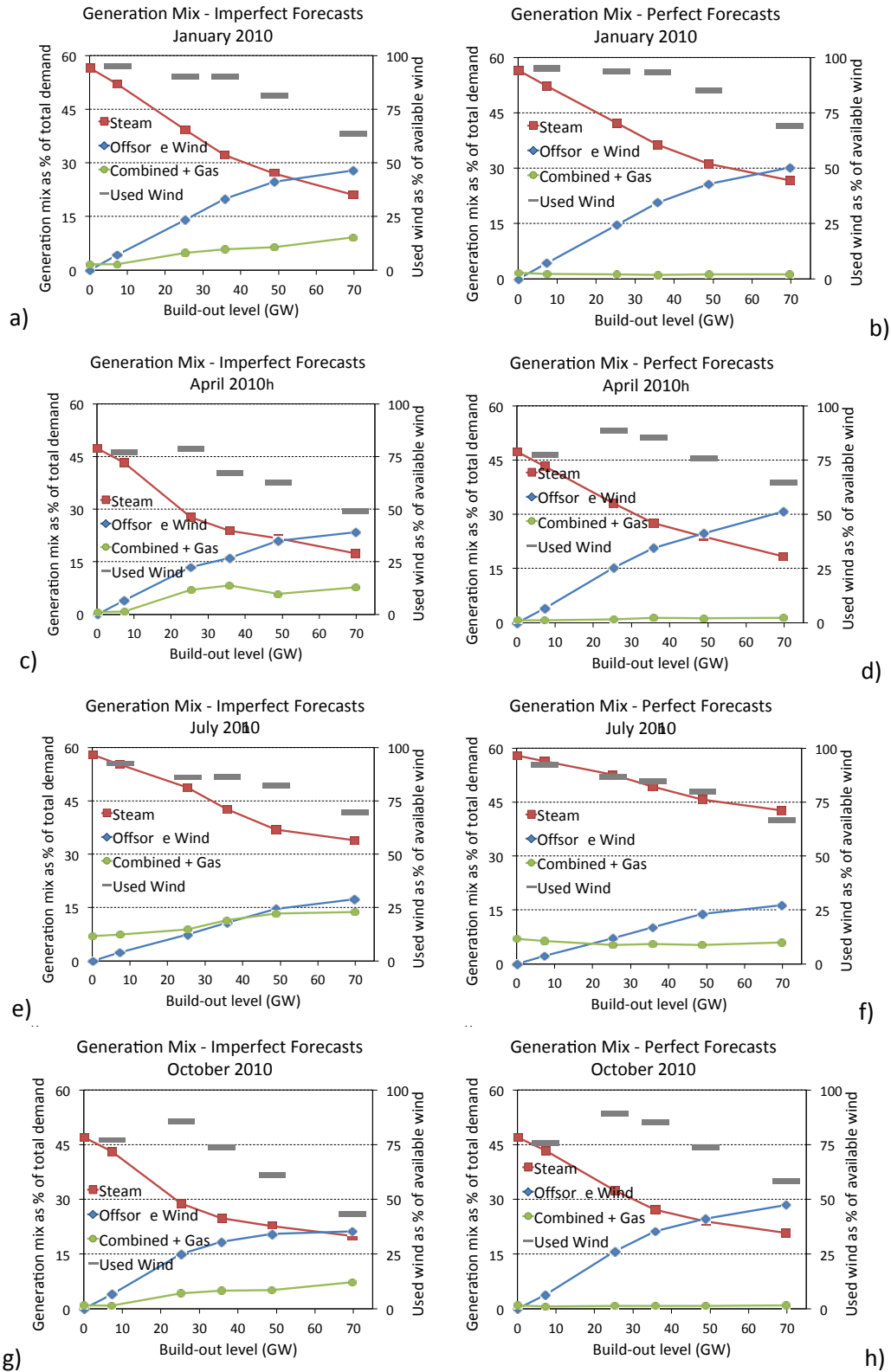
385

386 **Figure 8: Total simulated power, actual load, and wind during a 35-minute generation shortfall event**  
 387 **caused by an unexpected, sharp decrease in actual wind that was not predicted by either the day-**  
 388 **ahead forecast (DA-Predicted) or the short-term forecast (IT-Predicted).**

389 Figure 9 shows plots with the generation mix on the left-hand vertical axis and used wind as a  
 390 percentage of available wind on the right-hand vertical axis. In the generation mix we display the  
 391 percentage of energy produced by steam generators, combined-cycle/gas-turbines and offshore wind  
 392 farms only, since these are the forms of generation that are mostly affected by the introduction of  
 393 offshore wind. The plots on the left column depict the results for the case of imperfect forecasts,  
 394 whereas the ones on the right column depict the ones for perfect forecasts.

395 The main difference between the imperfect and perfect forecast cases is the usage of combined-  
 396 cycle/gas-turbines. In the imperfect case, this usage progressively increases with the wind build-out  
 397 level, as *fast* (gas) generators are employed more as the additional reserve needed to guarantee the  
 398 generation shortfall-free operation of the system. In the case of perfect forecasts, though, the usage of  
 399 combined-cycle/gas generation remains essentially flat with the wind build-out, since *slow* (steam)  
 400 generation can be used to balance the variability of wind.

401 We also note that wind utilization tends to decrease at higher penetration levels. As wind increases, we  
 402 need a larger number of dispatchable generators running at their minimum operational levels, in order  
 403 to guarantee that the system will be free of generation shortfalls when the wind power varies. As a  
 404 result, we end up using less of the available wind. Also, for the same level of wind *and* for the shoulder  
 405 months (that is, the times of the year when the difference between lowest and highest demand within a  
 406 day is smaller), perfect wind forecasts tend to produce higher wind usage than imperfect forecasts.



407 **Figure 9** Generation mix and percentage of wind used for the cases of imperfect (left column) and  
 408 **perfect (right column) wind forecasts. The right axis is the reference for Used Wind.**

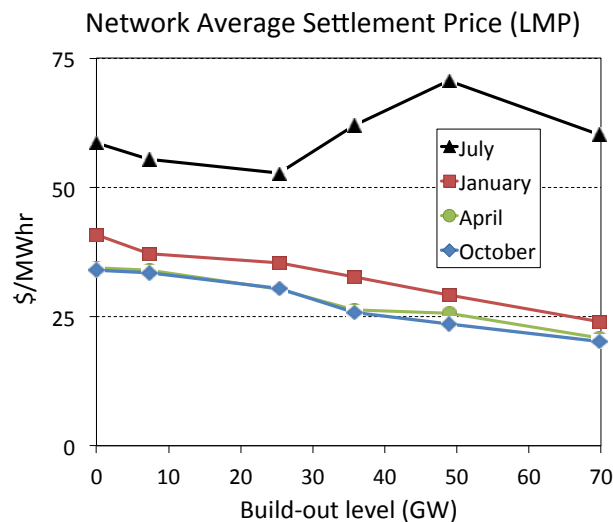


### 4.3 Impact on settlement prices and emissions

At least two additional questions arise from the trends observed in the generation mix as the levels of wind power in the system increase: (1) what is the overall impact on the network average settlement price (based on LMPs), and (2) what is the impact on the emission of air pollutants?

Figure 10 shows that the settlement price paid to generators by PJM (averaged over all generators) decreases as the level of offshore wind power in the system increases. Note also that the prices for build-out levels 4 and 5 in the summer season (July) have been affected by the penalties imposed for the observed generation shortfall. Both in the unit commitment and in the economic dispatch models, we use large penalties to curb demand shortage, rather than hard constraints. Consequently, when the solution of those optimization problems does involve generation shortfall, the marginal value of additional available generation – the LMPs – will be artificially inflated by the active penalties.

It is important to recognize that the reduction in the LMP is not necessarily proportional to total consumer or wholesale electricity savings – for example, it does not include capital cost of either existing generation or new wind generation, which would be reflected in the capacity market. To understand consumer savings, we would need to understand the relative effects of the cost savings shown in Figure 10 against the cost of energy from new wind generation and transmission. To understand the costs or savings to society, we would need to understand those factors as well as the social costs and savings of externalities such as health damages due to pollution reductions, like those itemized below. These total economic calculations are beyond the scope of the present study.

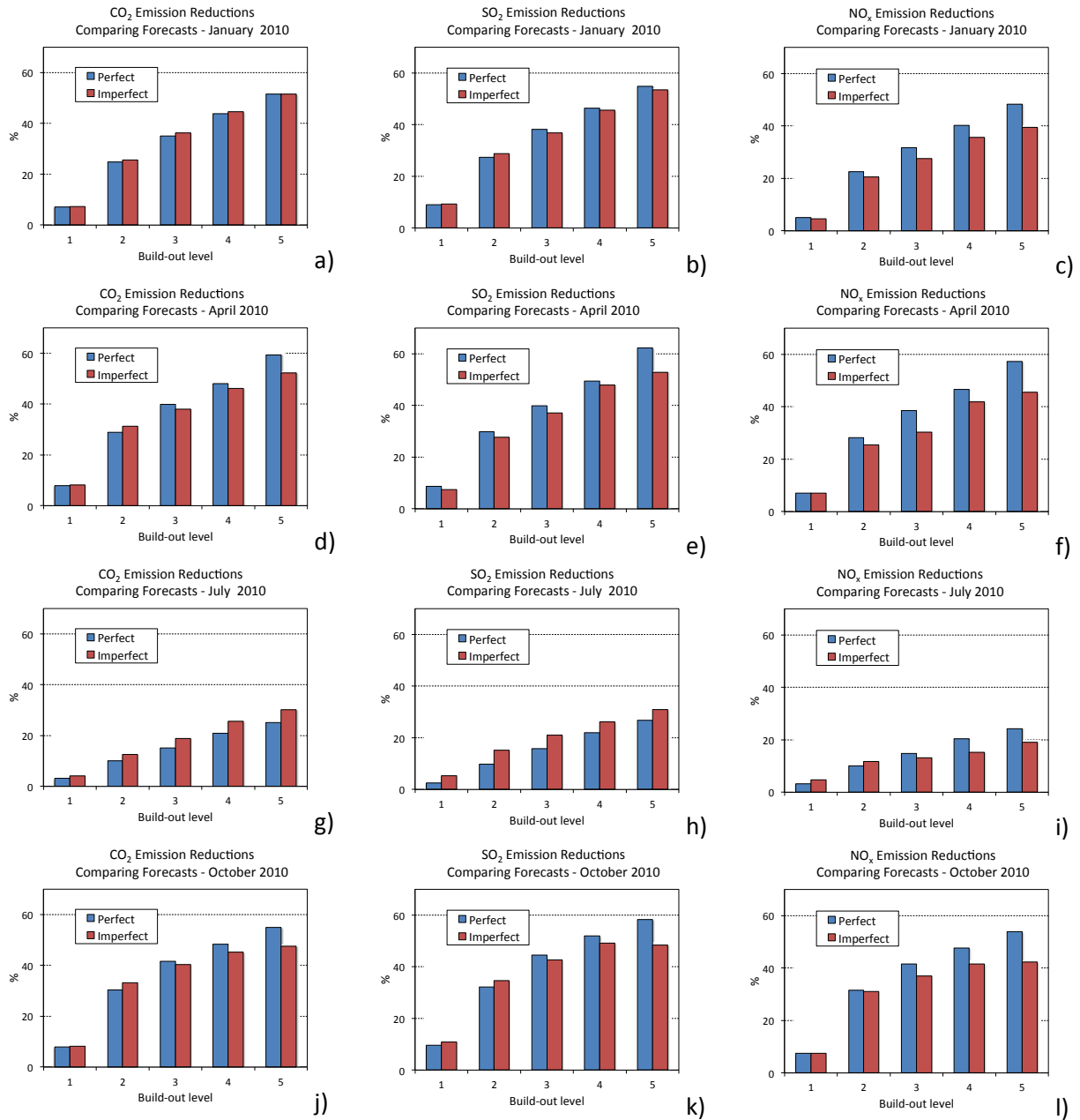


428

429 **Figure 10 Network average settlement price for the cases of imperfect wind forecasts and added**  
 430 **ramp-up and -down reserves by month.**

431 Figure 11 shows the reduction in emissions of carbon dioxide (CO<sub>2</sub>), sulfur dioxide (SO<sub>2</sub>) and nitrogen  
 432 oxides (NO<sub>x</sub>), three of the main air pollutants released in the burning of fossil fuels for the generation of  
 433 electricity. As expected, the higher the levels of wind power in the system, the greater the reduction in

434 the emission of these three pollutants. Furthermore, perfect forecasts yield higher reductions in  
 435 emissions than imperfect forecasts.



436 **Figure 11 Emission reductions of air pollutants (CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>x</sub>) for the cases of imperfect and**  
 437 **perfect wind forecasts.**

438 Table V summarizes the estimates in the reduction of settlement prices and emissions resulting from the  
 439 introduction of the several build-out levels of offshore wind power, obtained with imperfect level  
 440 forecasts.

441 **Table V: Summary of reductions in settlement prices and emissions for the case of imperfect wind**  
 442 **forecasts**

Build-out Level	Installed Capacity (GW)	Month-Year	Generation from Offshore Wind (%)	Network Average Settlement Price Reduction (%)	CO <sub>2</sub> Emission Reduction (%)	SO <sub>2</sub> Emission Reduction (%)	NO <sub>x</sub> Emission Reduction (%)
1	7.3	Jan-10	4	9	7	9	5
		Apr-10	4	2	8	7	7
		Jul-10	2	5	4	5	5
		Oct-10	4	1	8	11	8
2	25.3	Jan-10	14	13	26	29	21
		Apr-10	14	12	31	28	25
		Jul-10	8	10	13	15	12
		Oct-10	15	10	33	35	31
3	35.8	Jan-10	20	20	36	37	28
		Apr-10	16	24	38	37	30
		Jul-10	11	-6	19	21	13
		Oct-10	18	24	40	43	37
4	48.9	Jan-10	25	28	45	46	36
		Apr-10	21	26	46	48	42
		Jul-10	15	-20	26	26	15
		Oct-10	21	31	45	49	42
5	69.7	Jan-10	28	41	52	54	40
		Apr-10	23	39	52	53	46
		Jul-10	18	-3	30	31	19
		Oct-10	21	41	48	49	42

443

444 We note that the average settlement prices for the month of July, for build-out levels 3 and above  
 445 actually increased, rather than decrease. This is probably due, at least partially, to the significantly  
 446 higher levels of usage of the more expensive *fast* generation as reserves. The addition of generation  
 447 shortfall penalties in build-out levels 4 and 5 may also have contributed to further inflate the settlement  
 448 prices.

449 Wind build-out level 3, corresponding to an installed offshore capacity of 35.8 GW, is the highest  
 450 capacity at which we estimate the current PJM market can operate without any generation shortfall,  
 451 *with* additional ramping reserves *and* an unconstrained transmission grid. For this level, depending on  
 452 the season of the year, we obtained the following estimates:

- 453 • Energy from wind would satisfy between 11 and 20% of the demand for electricity;
- 454 • Settlement prices could be reduced by up to 24% (though in the peak summer season they may  
 455 actually increase by up to 6%);
- 456 • CO<sub>2</sub> emissions are reduced between 19 and 40%;
- 457 • SO<sub>2</sub> emissions are reduced between 21 and 43%;
- 458 • NO<sub>x</sub> emissions are reduced between 13 and 37%.

#### 459 **4.4 Constrained grid, no ramp-up or -down reserves added**

460 We were also interested in evaluating the capacity of the PJM system to integrate the various build-out  
 461 levels of offshore wind power with the transmission grid constrained by its current thermal capacities.

462 Two particular scenarios of connection between the offshore wind farms and the six onshore points of  
463 interconnection (POI) were tested:

- 464 • HVDC scenario - We envisioned the existence of a high-voltage DC (HVDC) backbone line under  
465 the sea, along the continental shelf of the Mid-Atlantic coast. The farms would be connected to  
466 this line, which in turn would be connected to the six POIs. Because new multi-terminal HVDC  
467 technologies are fully switchable, this scenario implies that each and every wind farm would be  
468 connected to each and every POI, and energy would thus be injected in the POI where needed.
- 469 • AC radial scenario - We envisioned each farm being connected by an AC radial line to one POI  
470 only, the nearest one geographically.

471 The HVDC backbone line, the AC radial lines and the POIs themselves were assumed to have thermal  
472 capacities sufficiently large that they did not constrain transmission.

473 Table VI shows statistics for the runs with the constrained grid and the HVDC backbone connection.  
474 They can be directly compared to those displayed in Table III for the unconstrained case. For build-out  
475 level 1, the amounts of wind power used in the constrained grid case, as a percentage of the total  
476 amount available in each season, are comparable to those in the unconstrained case; and so are the  
477 percentages of demand that are satisfied by electricity generated from offshore wind. This means that  
478 the injection of these relatively modest amounts of offshore wind power (between 2.4 and 4.0% of total  
479 demand, depending on the season) do not exceed the transmission grid capacities. We note that the  
480 generation shortfall observed at this level could be easily taken care of by the addition of some  
481 synchronized ramp-up and down reserves; the average peak generation shortfall, when there is any  
482 shortfall, depicted in Table VI, offers good initial estimates of what these reserves should be.

483 As we move to build-out levels 2 and beyond, offshore wind power becomes severely curtailed by the  
484 current grid capacity constraints, as indicated by the percentage of used wind, which drops to between  
485 37.8 and 60.7%, as opposed to the 86.9 to 93.4% range observed in the unconstrained case. This issue  
486 can only be resolved by an upgrade in the onshore transmission lines, particularly in the coastal areas.  
487 Therefore, installing offshore wind capacity of 25.3 GW (level 2) or more, without upgrading the PJM  
488 transmission grid, would not allow integration or efficient use of these large offshore wind build-out  
489 levels.

490 Note also that, particularly for build-out levels 2 and 3, the likelihood that there will be generation  
491 shortfall is smaller than what was observed for the unconstrained grid case (Table III). This is due to the  
492 fact that less offshore wind power is being used in the constrained case, as a result of the wind power  
493 curtailment induced by the grid capacity constraints.

494 Finally, Figure 12 shows plots with the percentage of used wind obtained using the HVDC backbone and  
495 the AC radial connections to link the offshore wind farms with the onshore PJM grid. AC radial  
496 connections will cause significantly more spilling of offshore wind power (about 20% more for build-out  
497 level 1) than an HVDC backbone connection.

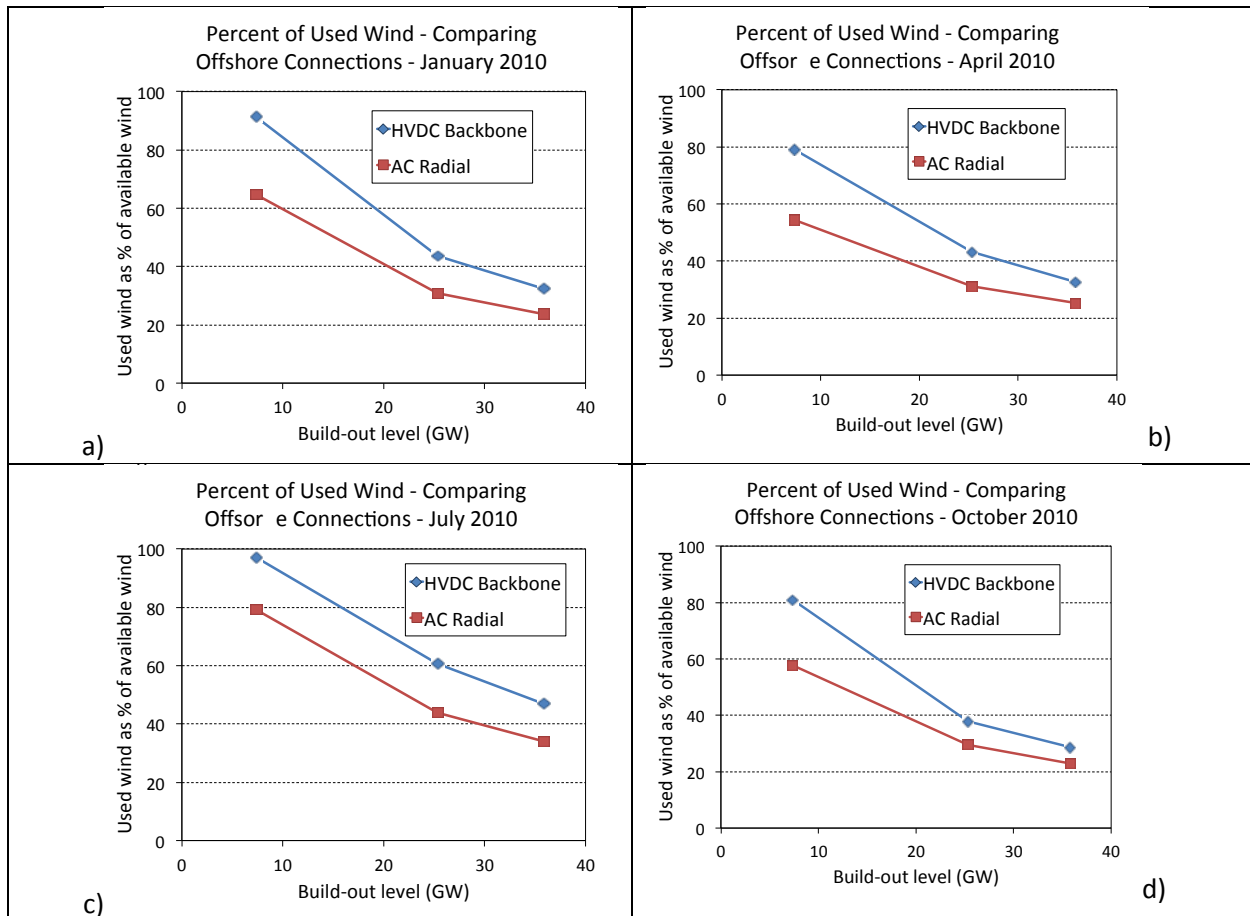
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499

**Table VI: Same as in Table III but for the constrained PJM grid with an HVDC backbone connection.**

Build-out Level	Installed Capacity (GW)	Month-Year	Generation from Offshore Wind (%)	Used Wind (%)	Likelihood There Will Be Generation Shortfall at Some Time During the Week (%)	Average Peak Generation Shortfall (GW), When There Is Any Shortfall
1	7.3	Jan-10	4.1	91.3	47.6	0.7
		Apr-10	4.0	79.1	9.5	0.4
		Jul-10	2.4	97.1	52.4	2.2
		Oct-10	4.2	81.2	0.0	0
2	25.3	Jan-10	6.8	43.7	47.6	1.0
		Apr-10	7.4	43.2	28.6	1.3
		Jul-10	5.0	60.7	100.0	3.3
		Oct-10	6.7	37.8	33.3	0.6
3	35.8	Jan-10	7.2	32.5	57.1	0.8
		Apr-10	8.0	32.6	38.1	1.0
		Jul-10	5.7	46.9	100.0	3.9
		Oct-10	7.2	28.7	52.4	0.9

500



501

**Figure 12 Percentages of used wind with HVDC-backbone versus AC-radial offshore connections.**

## 502 **5 Conclusions**

503 In this paper we showed that increasing amounts of offshore wind generation from the Mid-Atlantic  
504 section of the U.S. can be integrated into the PJM market, up to a certain level, provided that additional  
505 synchronized reserves be secured and that the transmission lines be upgraded (or in our model, that the  
506 grid be unconstrained). Furthermore, we also showed that improvements in the quality of the wind  
507 power forecasts used for both day-ahead and intermediate-term unit commitment planning have the  
508 potential to enable the integration of larger amounts of offshore wind power, with less amounts of  
509 required additional reserves.

510 Constrained by the current capacities of the onshore transmission grid, in the PJM market, we found  
511 that:

- 512 1. Up to about 7.3 GW of installed offshore wind capacity (build-out level 1) could be integrated,  
513 with required additional synchronized ramp-up and down reserves between 1 and 2 GW in the  
514 peak summer period.
- 515 2. Wind power curtailment would range from 3 to 21%, depending on the season of the year.
- 516 3. Using AC radial connections to link the offshore farms to the onshore grid, instead of an HVDC  
517 backbone connection, would cause an additional wind power curtailment on the order of 20%.

518 Assuming that the onshore transmission grid were appropriately upgraded by increasing the capacities  
519 of some lines, in the PJM market, we found that:

- 520 1. Up to about 35.8 GW of installed offshore wind capacity (build-out level 3) could be integrated,  
521 with required additional reserves of about 8 GW in the peak summer period (between 3 and 6  
522 GW in the other periods). These reserves range from 10 to over 20 percent of the installed wind  
523 generation capacity at build-out level 3.
- 524 2. In this scenario, offshore wind power would satisfy about 11% of the loads in the summer and  
525 an average of 18% in the other seasons of the year.
- 526 3. Wind curtailment would range from 10 to 33%, depending on the period of the year.

527 In the idealized case of having access to *perfect* wind power forecasts (that is, forecasts exactly equal to  
528 the observed wind power), the system would be able to handle up to 69.7 GW of installed offshore wind  
529 capacity (satisfying 16% of demand in the summer, and an average of 30% in the other seasons).

530 Finally, even with the addition of significant amounts of synchronized ramp-up and down reserves, we  
531 showed that integrating increasing amounts of offshore wind power will, in most cases, progressively  
532 lower the network-averaged settlement price of operating the PJM market, as well as consistently  
533 decrease the emissions of the three most important air pollutants associated with the burning of fossil  
534 fuels. More specifically, in the aforementioned case of integrating offshore wind power at build-out  
535 level 3, with additional reserves of up to 8 GW and an unconstrained onshore transmission grid:

- 536 • Settlement prices could be reduced by up to 24%;
- 537 • CO<sub>2</sub> emissions, between 19 and 40%;
- 538 • SO<sub>2</sub> emissions, between 21 and 43%; and

- 539
- NO<sub>x</sub> emissions, between 13 and 37%.

540 We believe that SMART-ISO represents, as of this writing, an accurate reproduction of PJM's dispatch  
541 planning process, with careful attention given to the modeling of the variability and uncertainty of wind.  
542 Of course, any model, or set of simulations, requires assumptions and approximations. The most  
543 significant assumption, in our view, is that we have focused on using existing planning and forecasting  
544 processes, as well as both existing generation technology and the current fleet of generators. We feel  
545 that we are now well-positioned to undertake studies that capture the effects of changes to this  
546 planning process and of improved forecasting, in addition to investments in existing and new  
547 technologies.

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